

| sets | vector spaces |
|---|--|
| S is a finite set | V is a finite-dimensional vector space |
| $\#S$ | $\dim V$ |
| for subsets S_1, S_2 of S , the union $S_1 \cup S_2$ is the smallest subset of S containing S_1 and S_2 | for subspaces V_1, V_2 of V , the sum $V_1 + V_2$ is the smallest subspace of V containing V_1 and V_2 |
| $\#(S_1 \cup S_2)$ $= \#S_1 + \#S_2 - \#(S_1 \cap S_2)$ | $\dim(V_1 + V_2)$ $= \dim V_1 + \dim V_2 - \dim(V_1 \cap V_2)$ |
| $\#(S_1 \cup S_2) = \#S_1 + \#S_2$ $\iff S_1 \cap S_2 = \emptyset$ | $\dim(V_1 + V_2) = \dim V_1 + \dim V_2$ $\iff V_1 \cap V_2 = \{0\}$ |
| $S_1 \cup \dots \cup S_m$ is a disjoint union \iff $\#(S_1 \cup \dots \cup S_m) = \#S_1 + \dots + \#S_m$ | $V_1 + \dots + V_m$ is a direct sum \iff $\dim(V_1 + \dots + V_m)$ $= \dim V_1 + \dots + \dim V_m$ |